

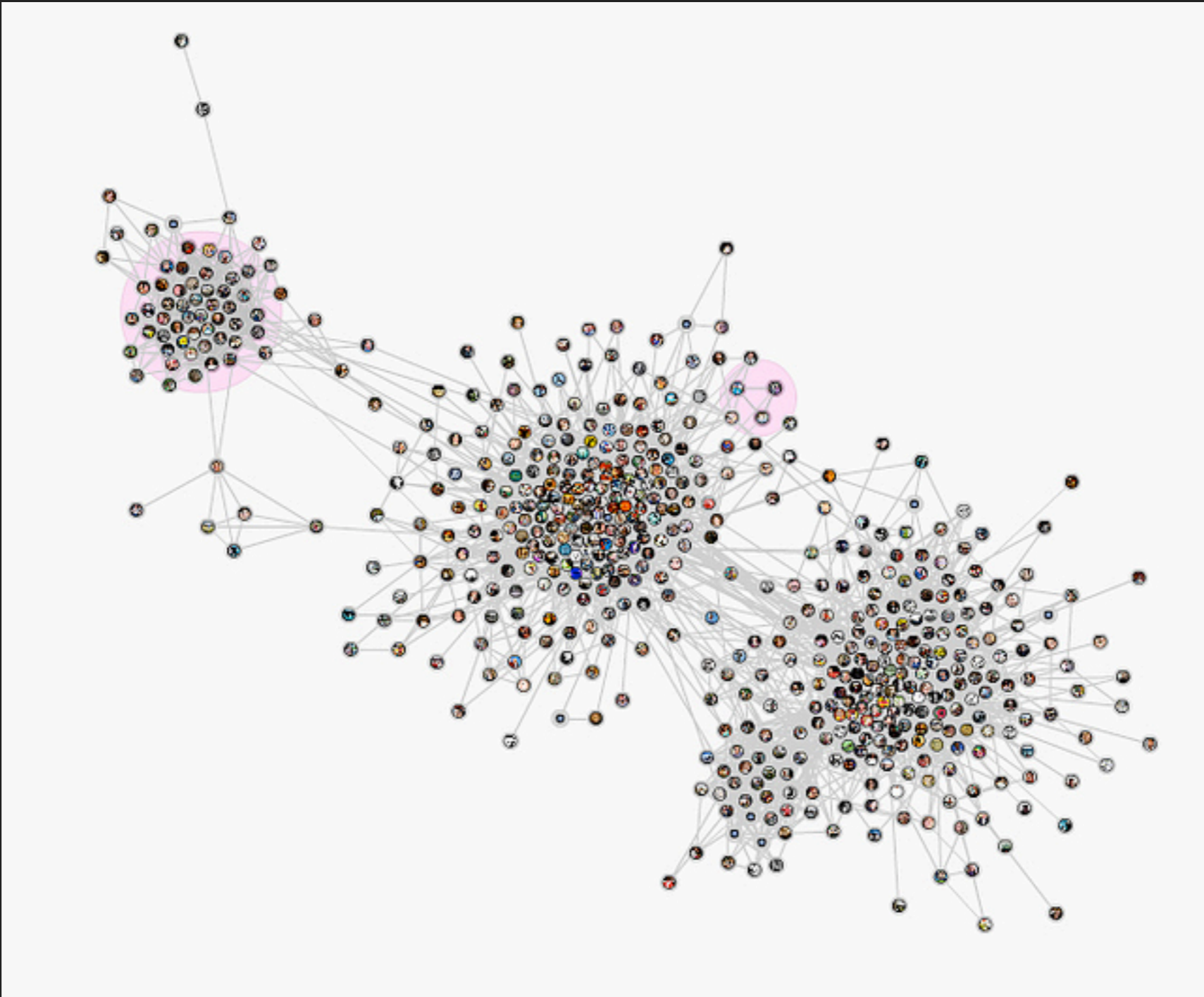
CSC 240

---

# GRAPHS

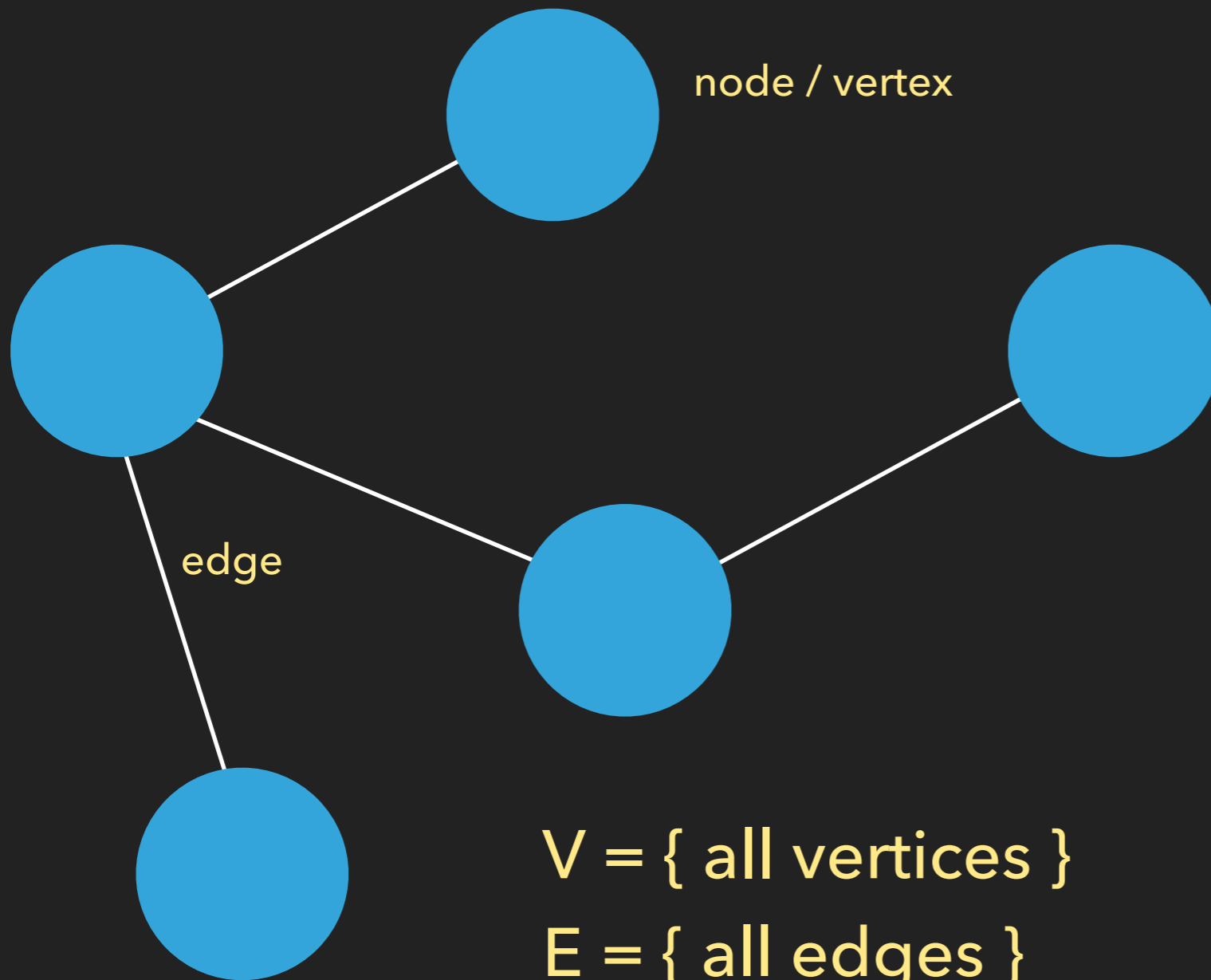
# GRAPHS

---



# GRAPHS

---



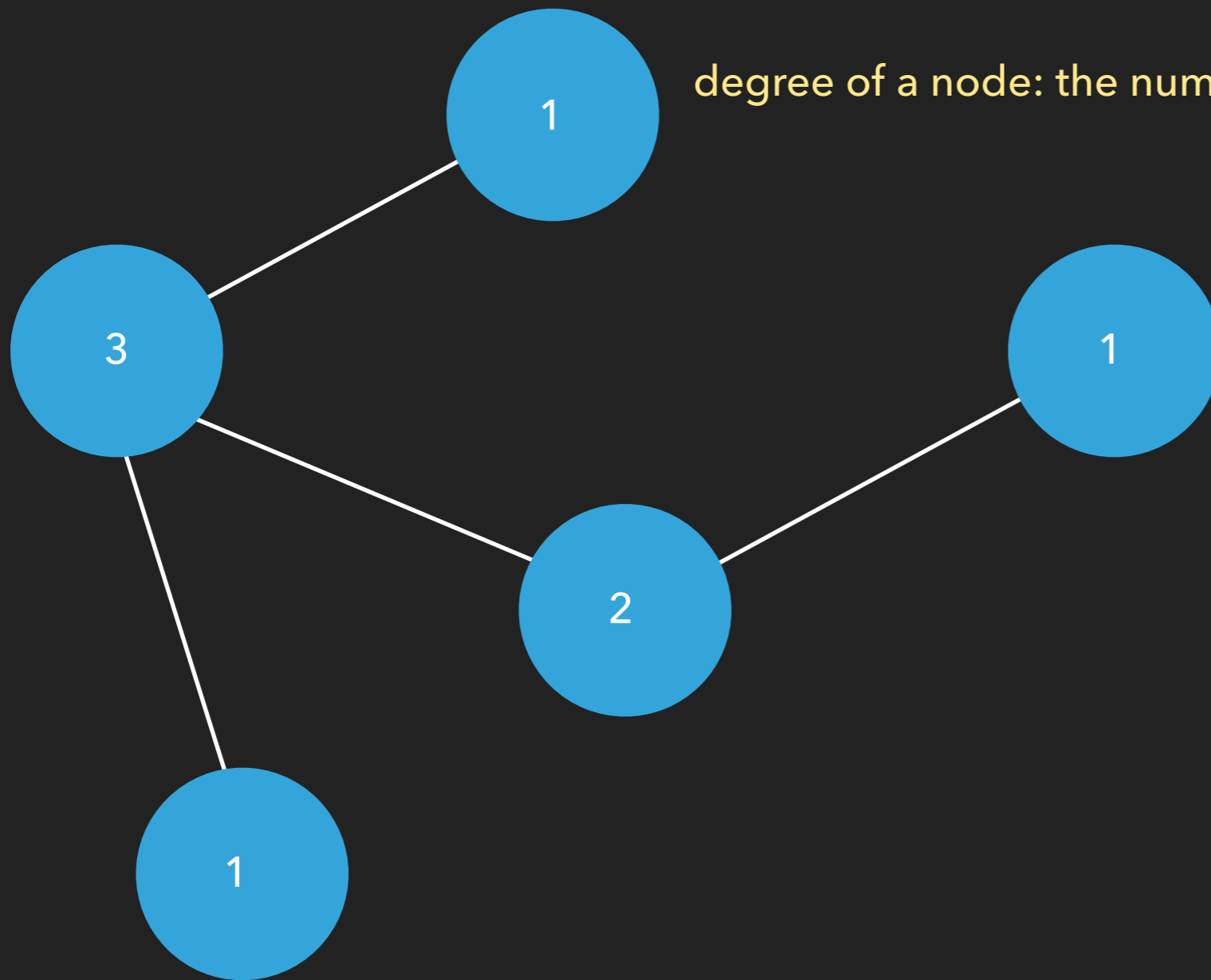
$V = \{ \text{all vertices} \}$

$E = \{ \text{all edges} \}$

$G = (V, E)$

# GRAPHS

---

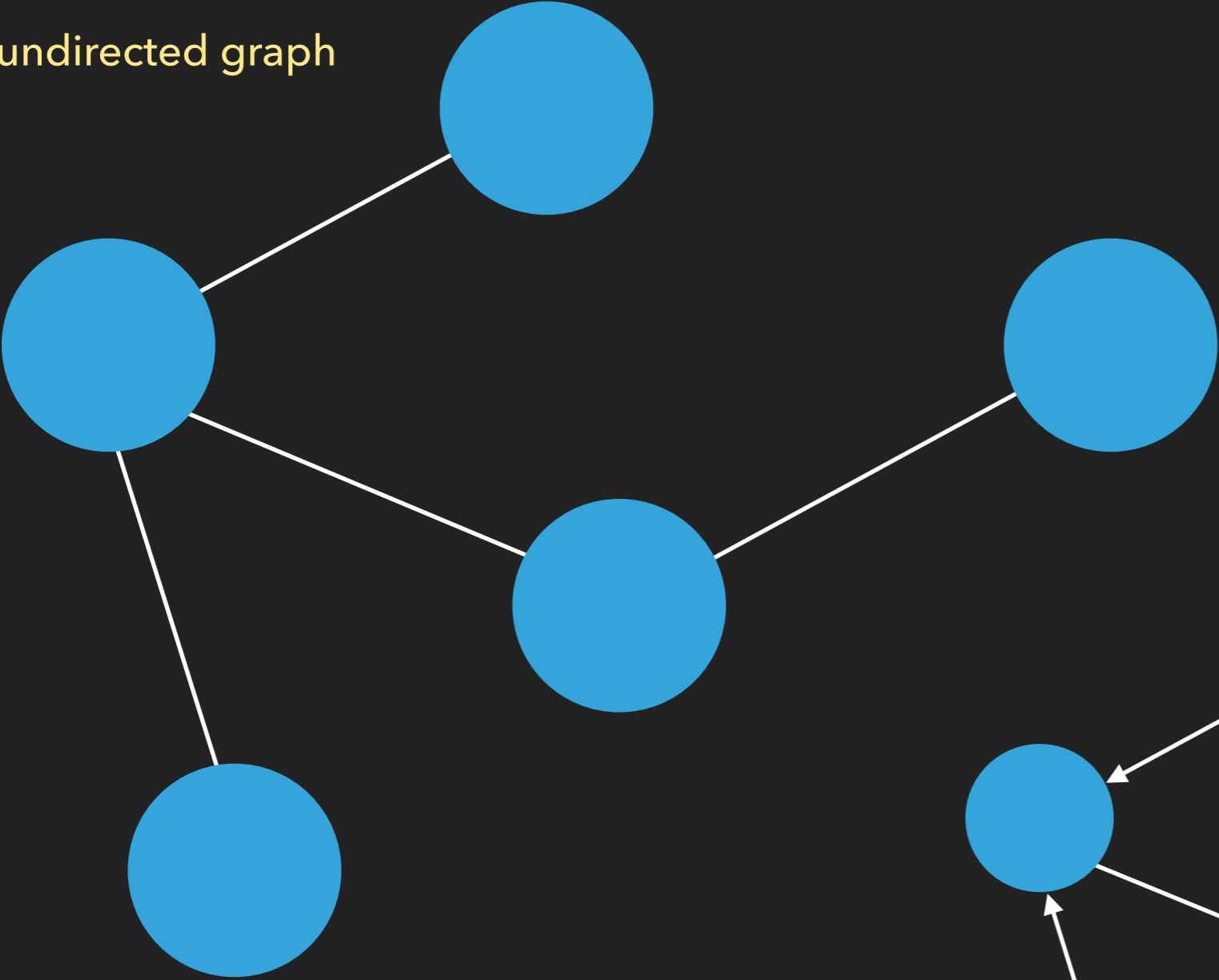


degree of a node: the number of edges connected to that node.

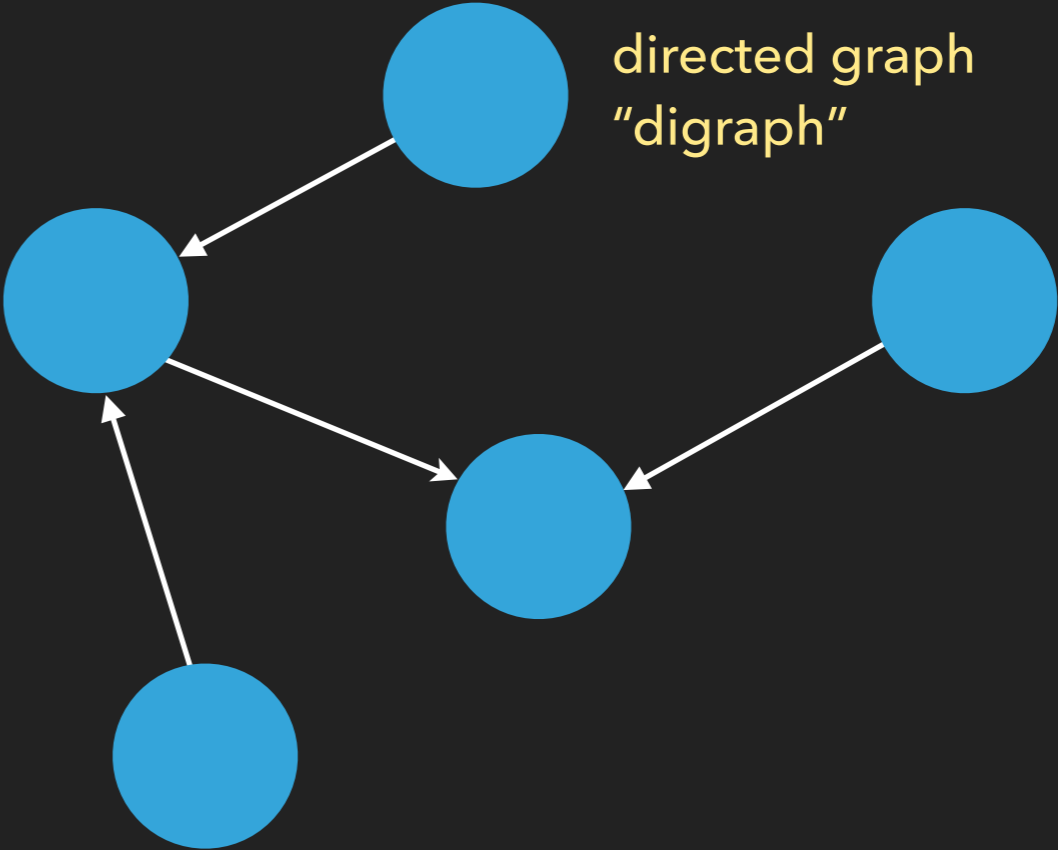
# GRAPHS

---

undirected graph

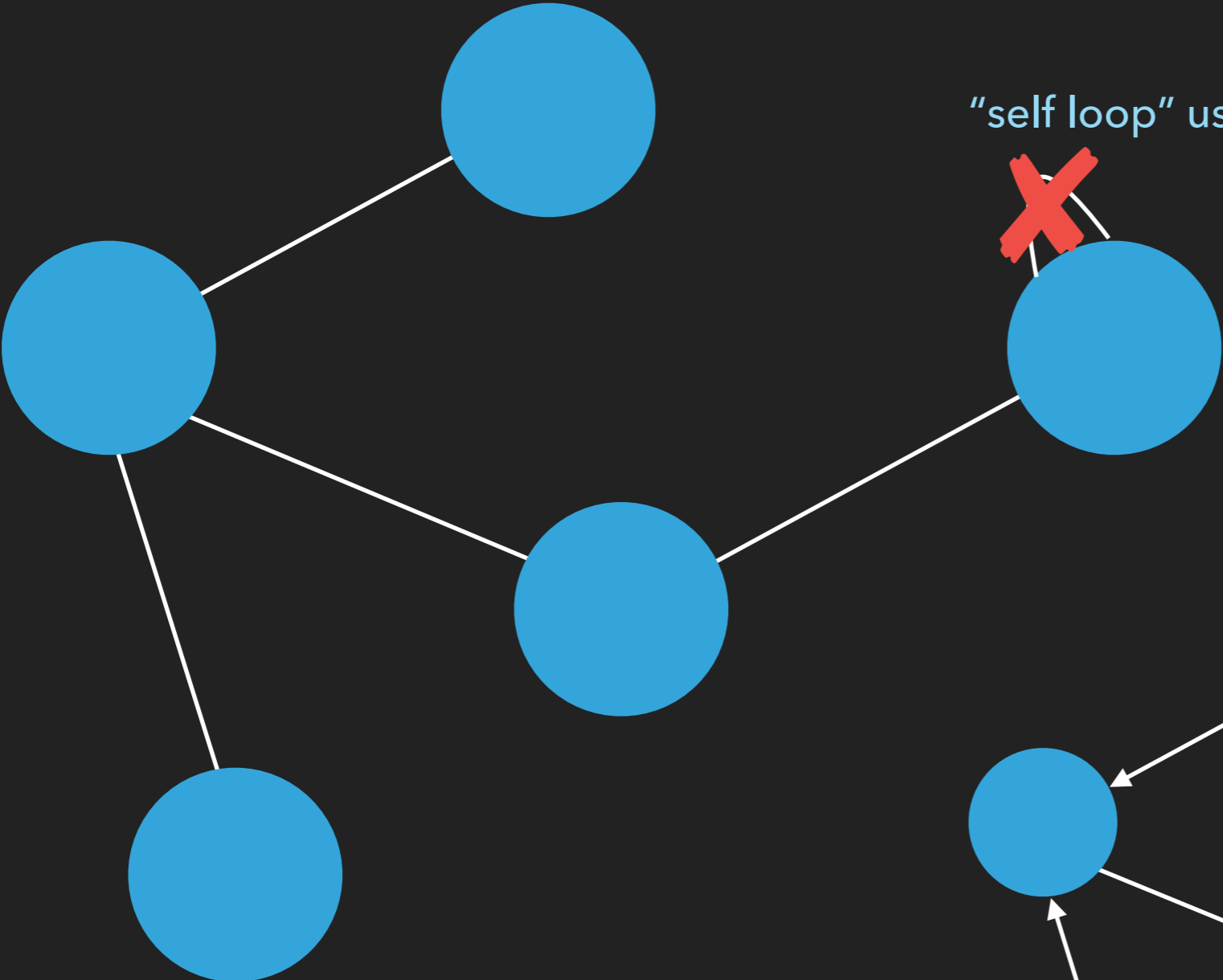


directed graph  
"digraph"

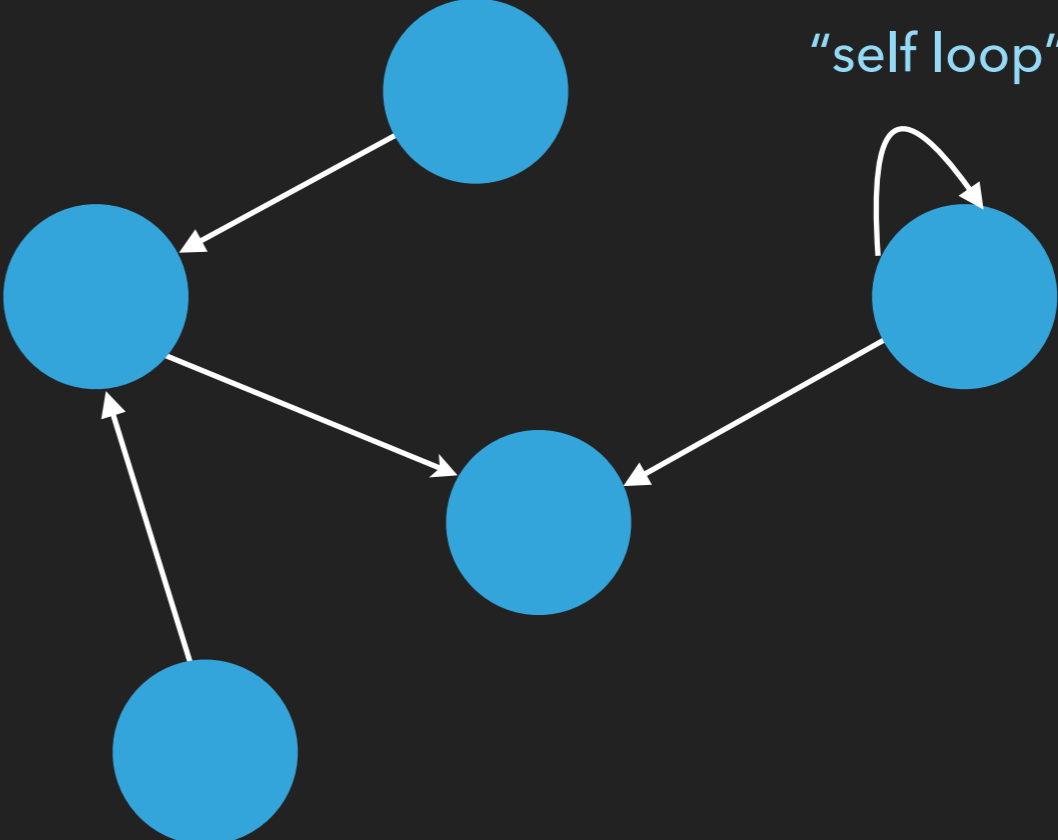


# GRAPHS

---



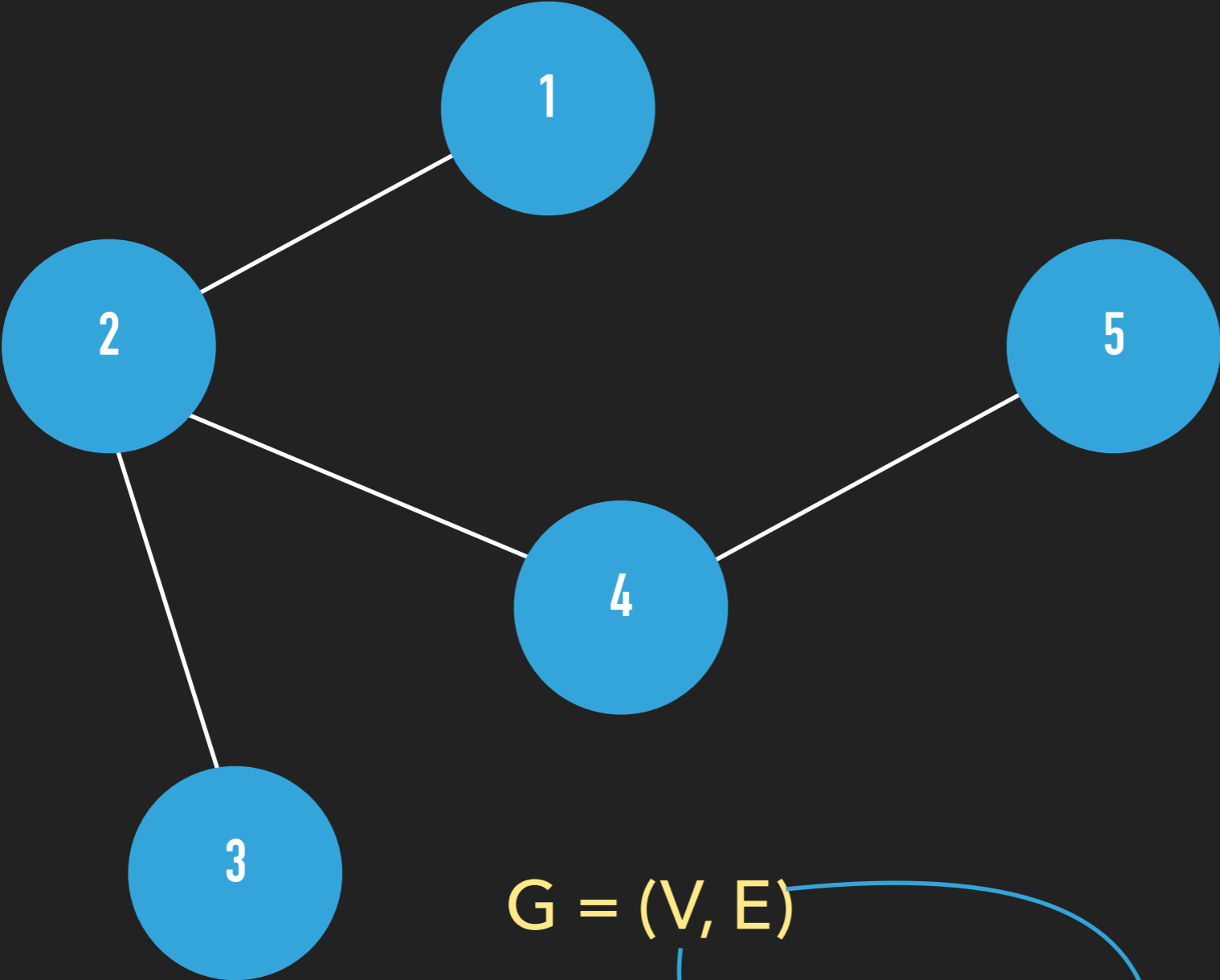
"self loop" usually not allowed in undirected graphs



"self loop"

# GRAPHS

---

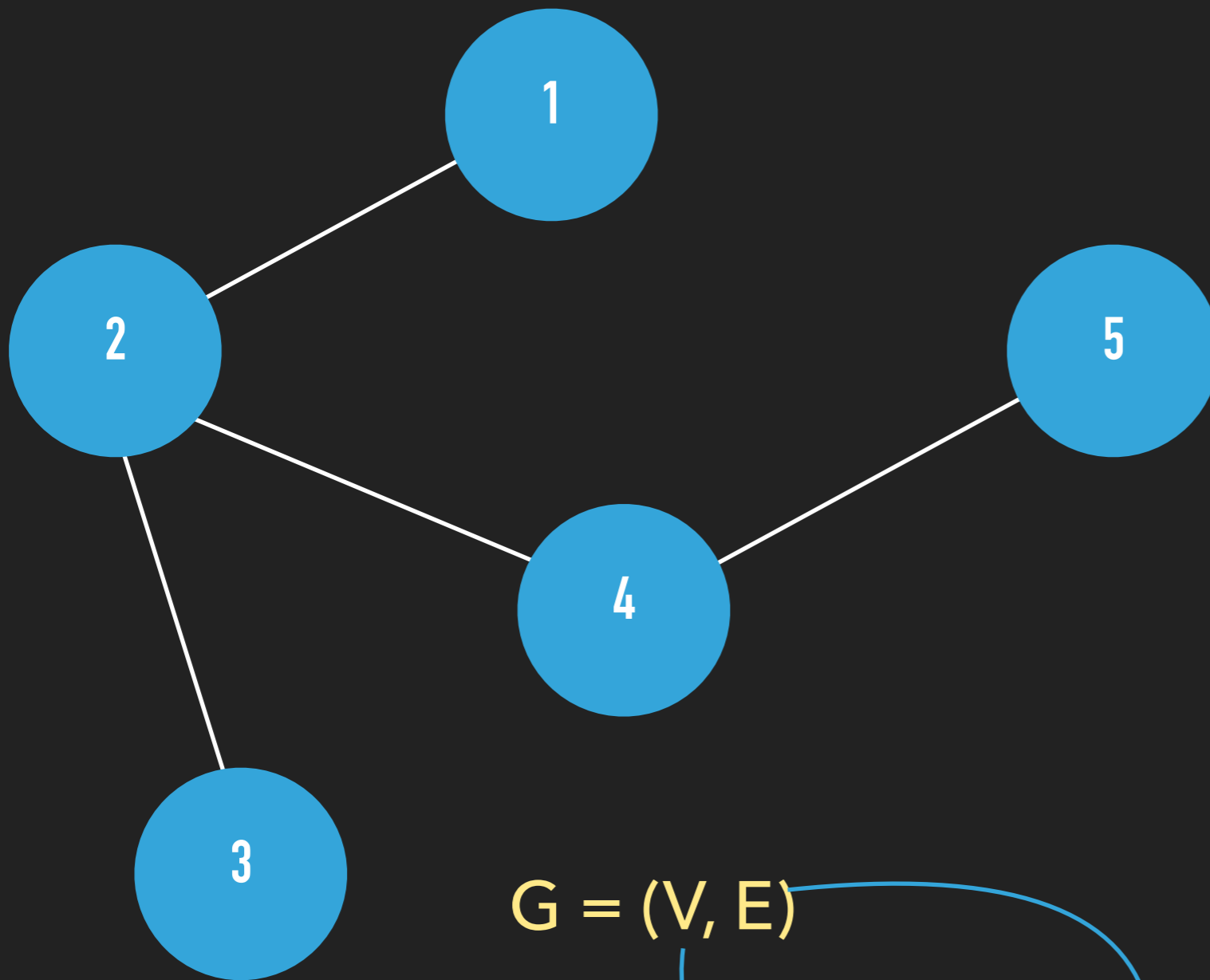


$$G = (V, E)$$

$$G = ( \{1, 2, 3, 4, 5\}, \{ \{1,2\}, \{2,3\}, \{2,4\}, \{4, 5\} \} )$$

# GRAPHS

---



$$G = (V, E)$$

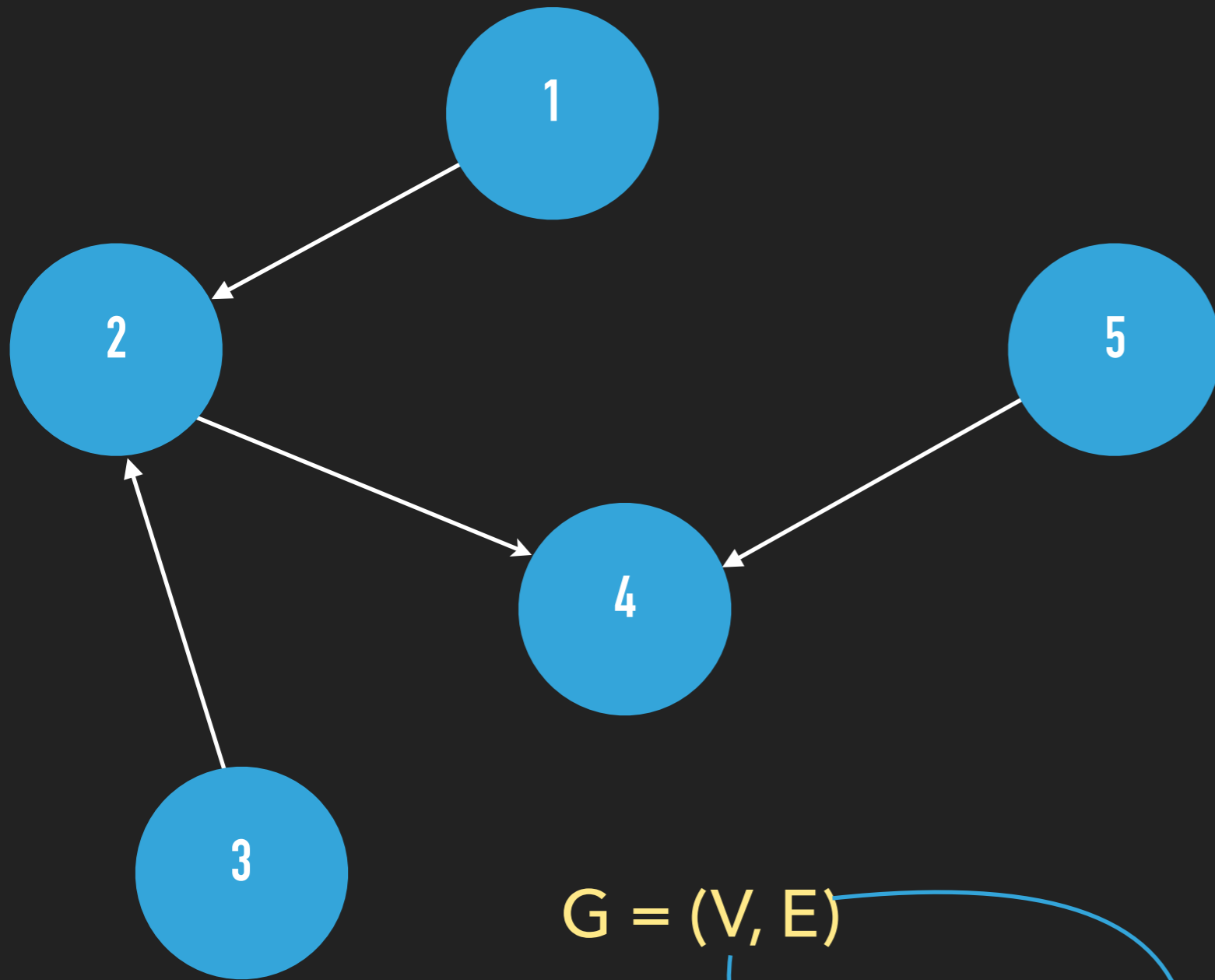
$$G = ( \{1, 2, 3, 4, 5\}, \{ \{1, 2\}, \{2, 3\}, \{2, 4\}, \{4, 5\} \} )$$

Notice that these are "unordered pairs"



# GRAPHS

---



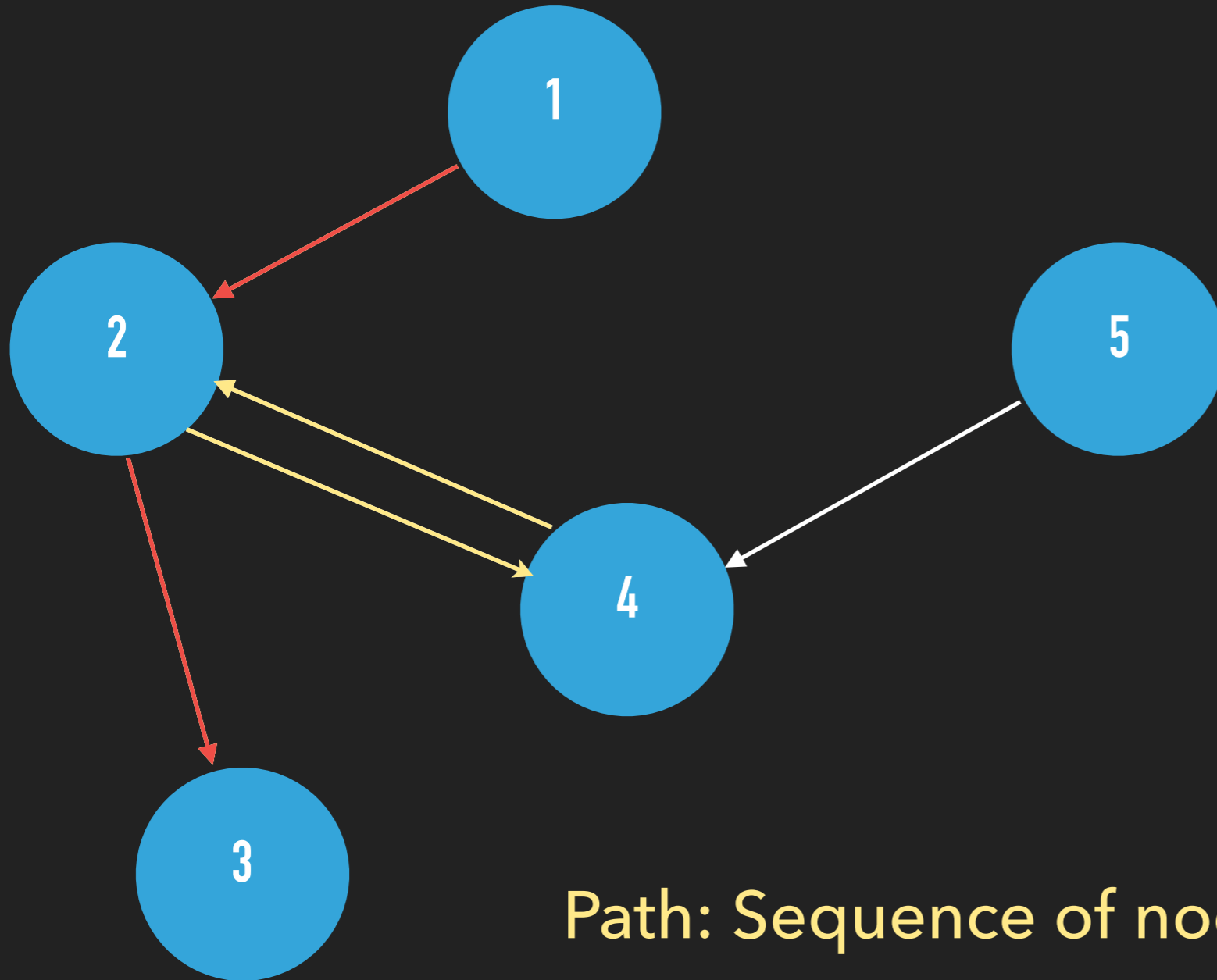
$$G = (V, E)$$

$$G = ( \{1, 2, 3, 4, 5\}, \{ (1,2), (3,2), (2,4), (5,4) \} )$$

Notice that these are "ordered pairs", following the order of the edge.

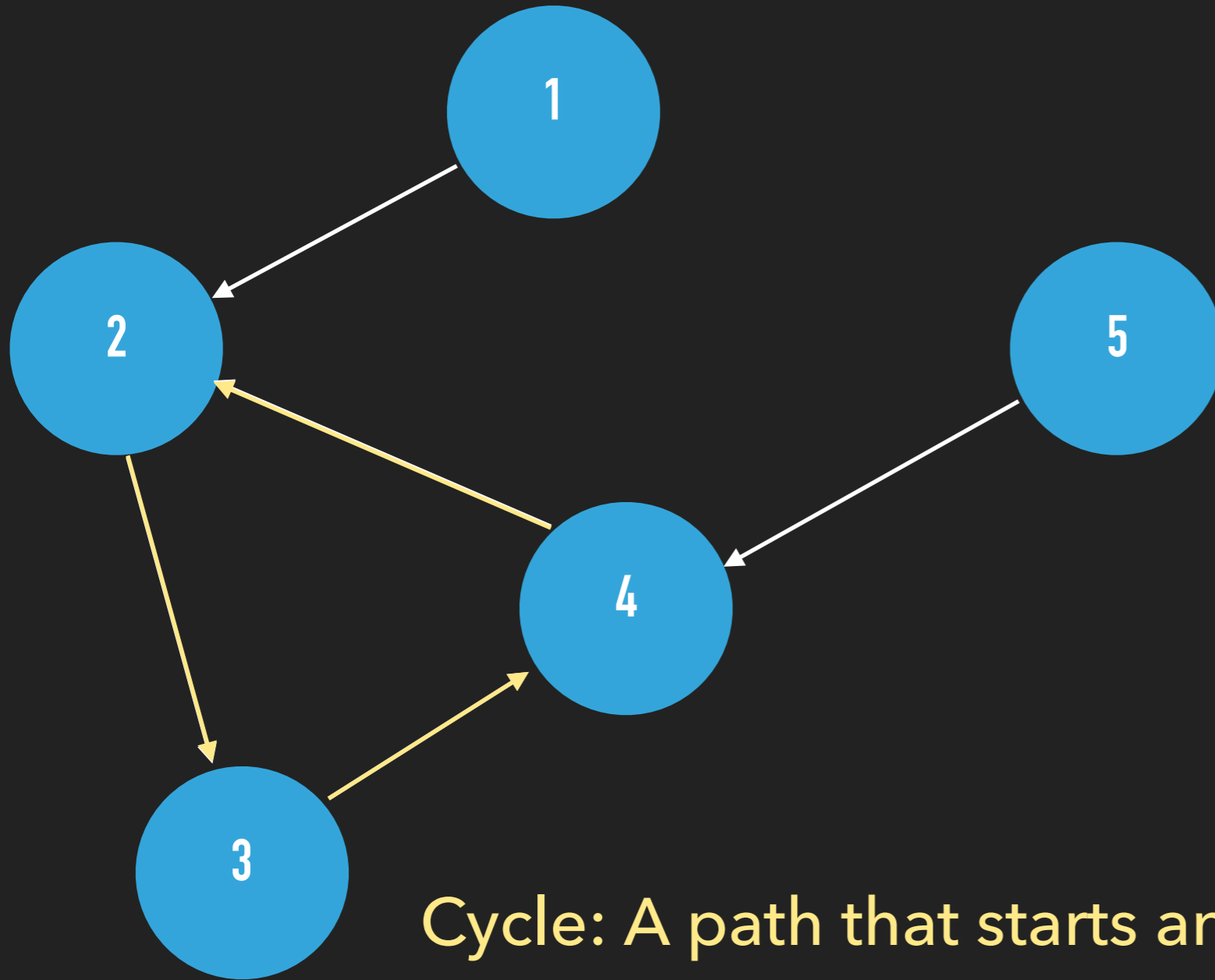
# GRAPHS

---



Path: Sequence of nodes connected by edges.  
(1, 2, 4, 2, 3)

Simple Path: A path with no repeated nodes.  
(1, 2, 3)

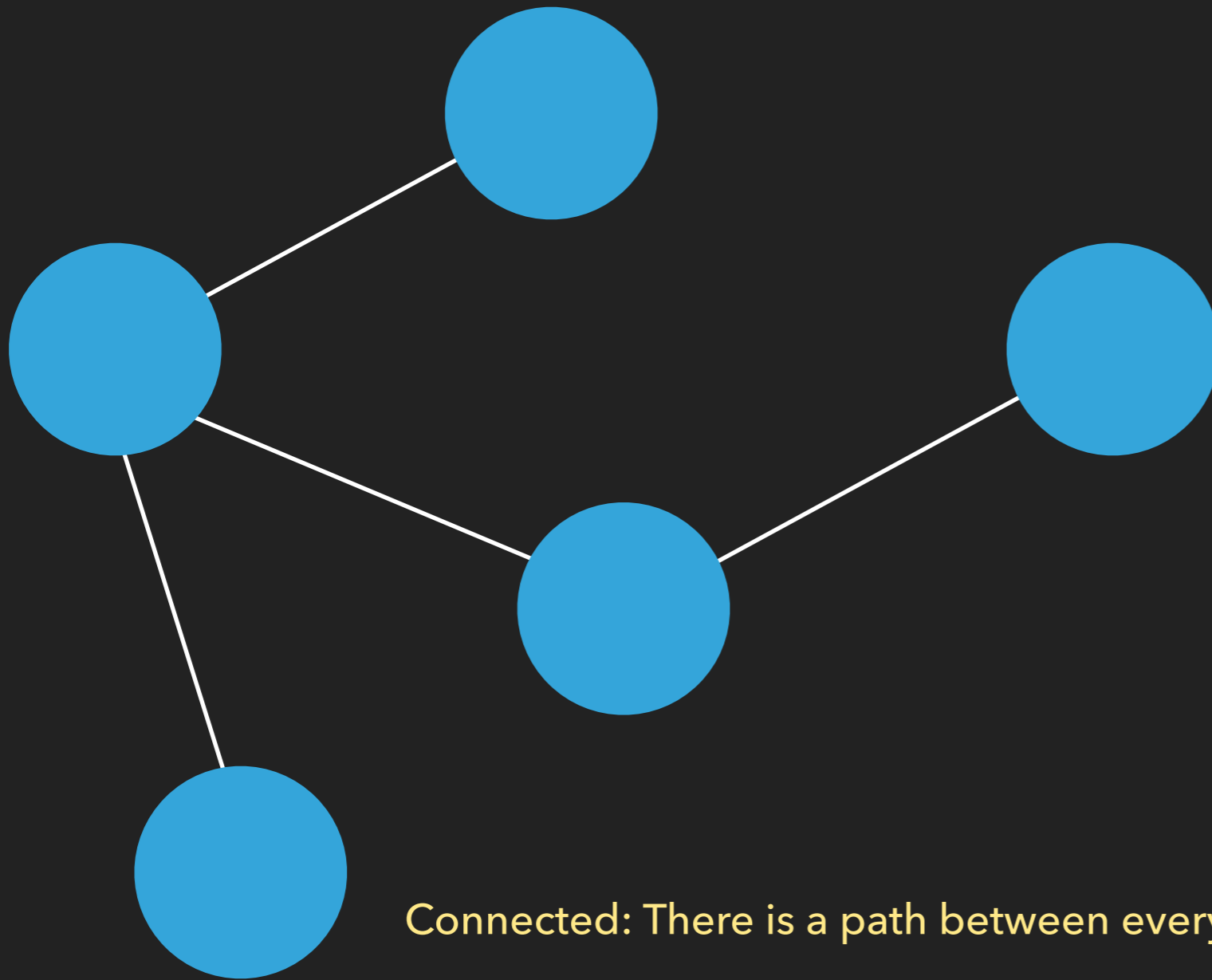


**Cycle:** A path that starts and ends at the same node.  
(2, 3, 4, 2)

**Simple Cycle:** A cycle with no repeated nodes except the first and the last.

# GRAPHS

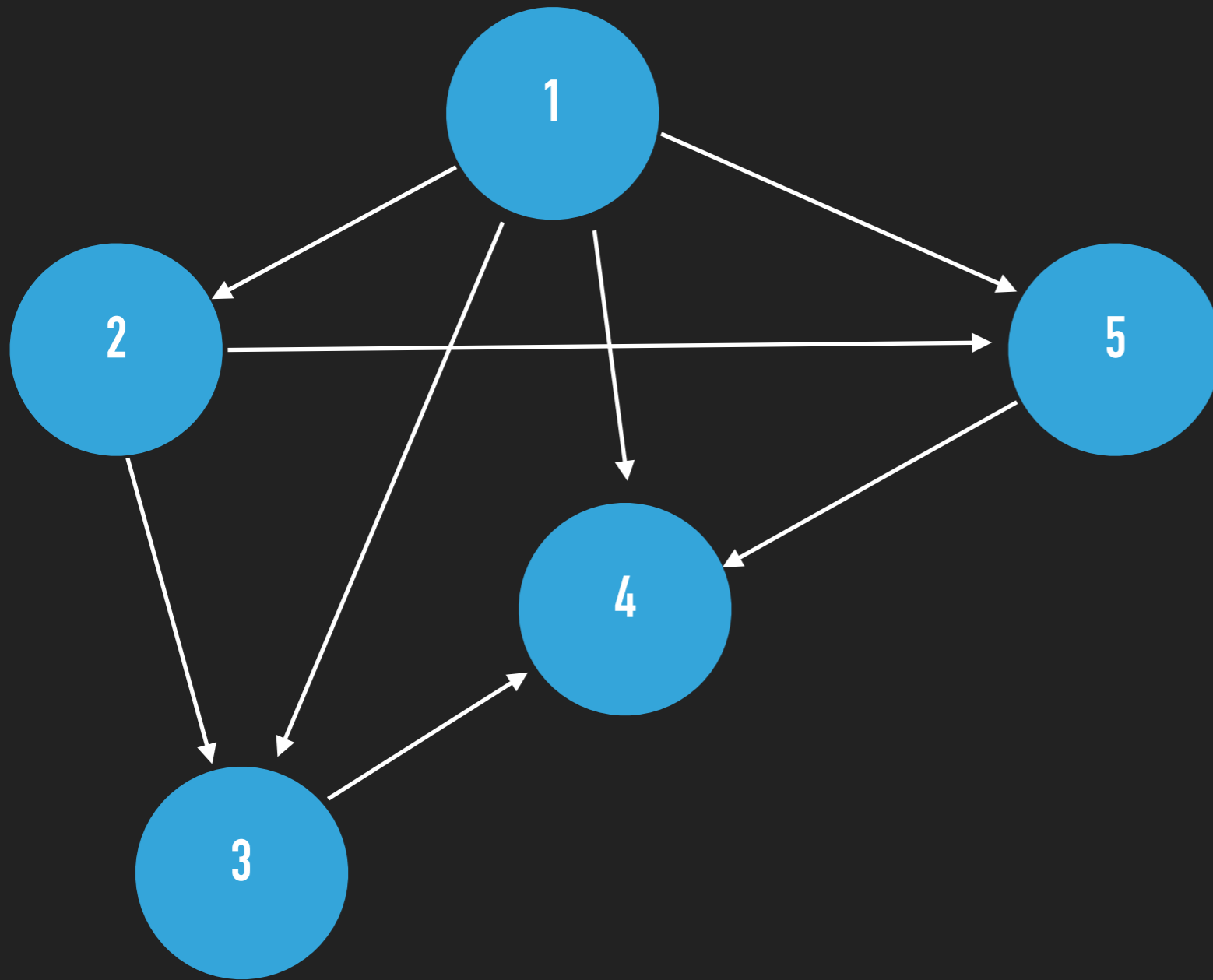
---



Connected: There is a path between every pair of nodes.

# GRAPHS

---

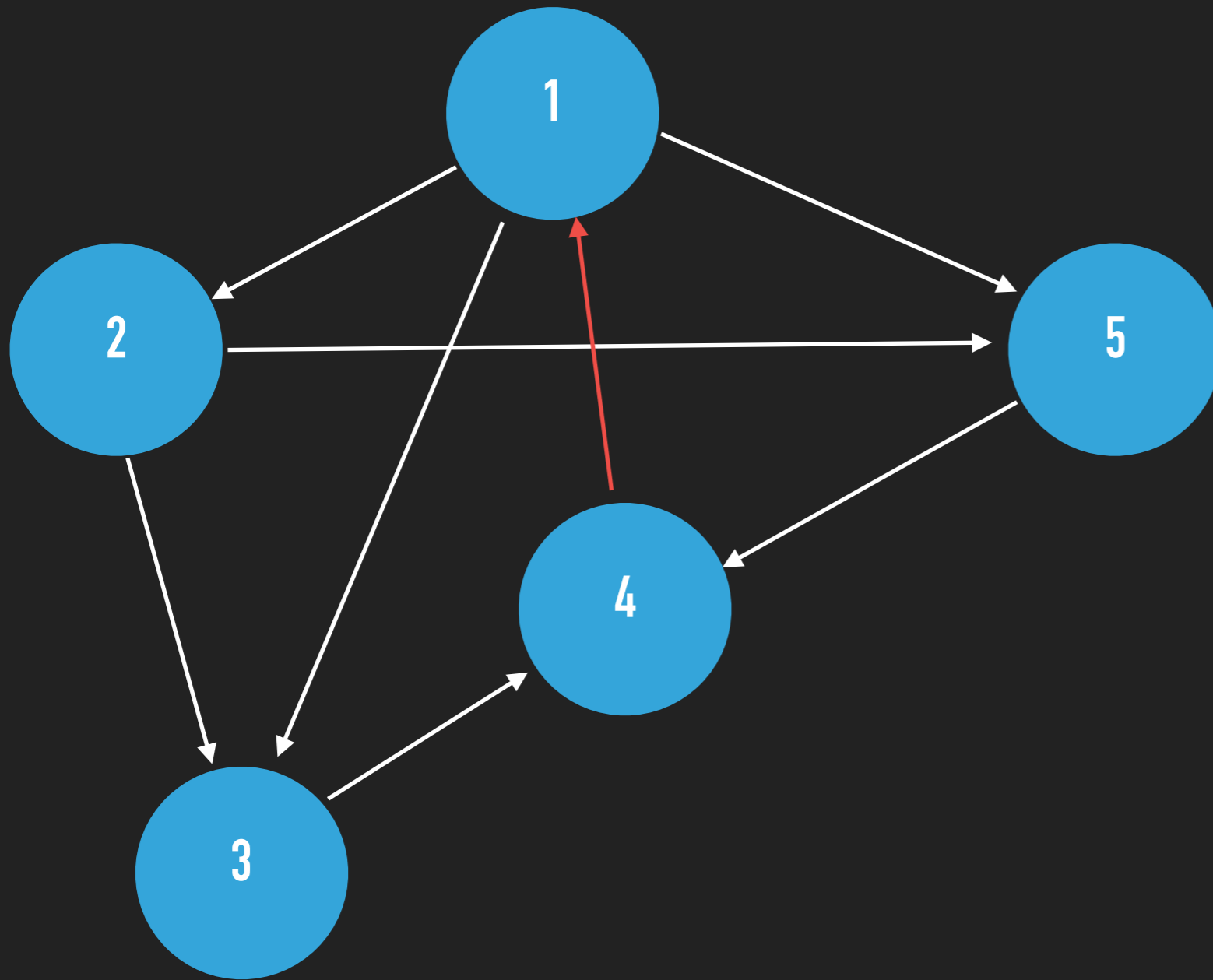


Strongly Connected: There is a **directed** path between every pair of nodes.

What needs to change about this graph to make it strongly connected?

# GRAPHS

---



Strongly Connected: There is a **directed** path between every pair of nodes.

What needs to change about this graph to make it strongly connected?